

Application of Finite-time Thermodynamics for Evaluation Method of Heat Engines

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Contents

- 1. Motivation & lessons**
- 2. Concept**
- 3. Normalization of TE**
- 4. Summary and future work**

- Established in 2003
- Over 40 years of experience of OTEC*
(*Ocean Thermal Energy Conversion)



<OTEC team:>

- System optimization
(Experimental, Computational)
- Heat exchanger development
(Performance test benches, visualization, CFD)



Ocean Thermal Energy Conversion System in Japan



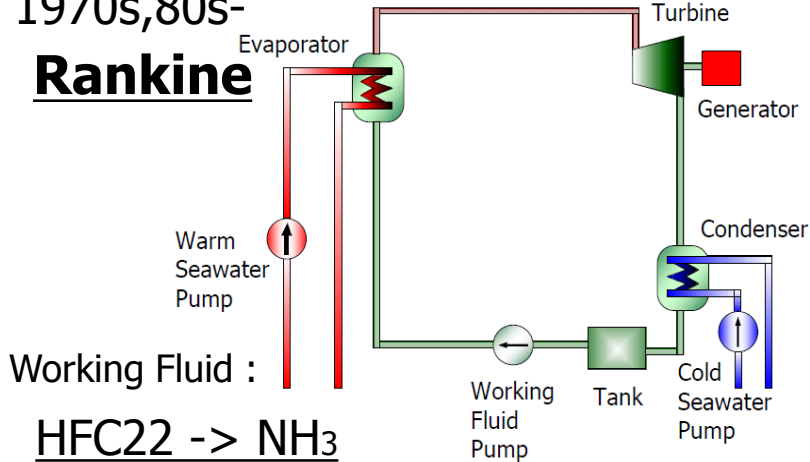
- 100kW
- HFC134a
- Rankine cycle (2-stages)

In 2013, launched **NEW STAGE** to connect the **grid** for the first time in the 21st century.

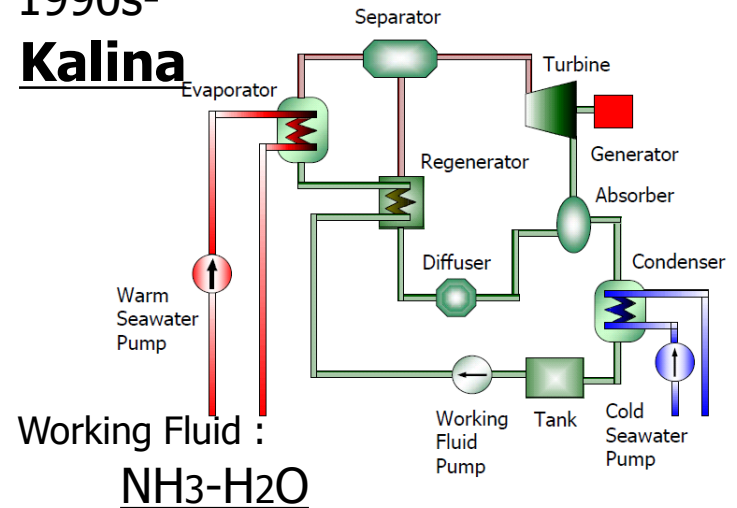
1. Motivation & lessons

Development of High Efficiency Thermo-Cycle

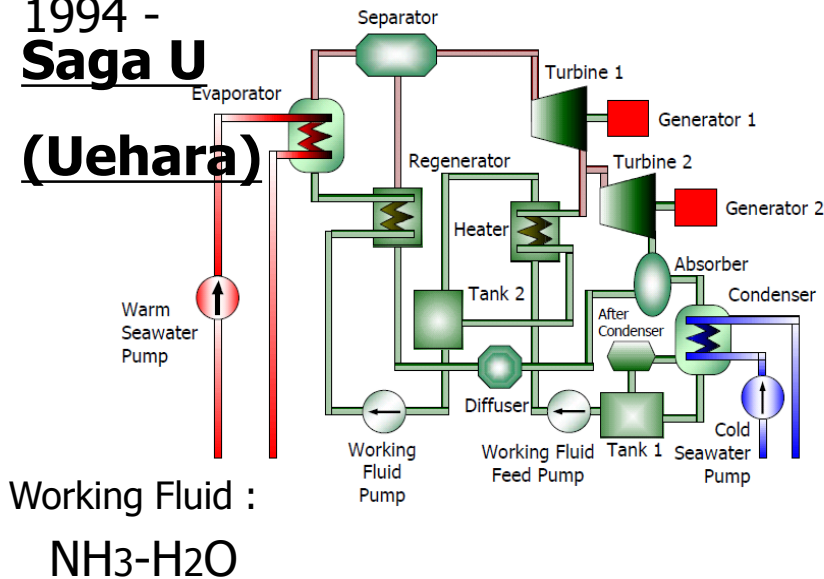
1970s,80s-
Rankine



1990s-
Kalina



1994 -
Saga U
(Uehara)



2011 - **Double Rankine**
NH₃
HFC134a

Increase Net power
NOT
Thermal efficiency

Thermal efficiency

*Avery, H. W. and Wu, C., Renewable Energy from the Ocean
- A guide to OTEC - (1994)*

- Upper bound of thermal efficiency:
Warm seawater temp T_W and
Cold seawater temp T_C

$$\eta_{th,m} = 1 - \frac{T_C}{T_W}$$

The half of Upper

$$\eta_{th,CA} = 1 - \sqrt{\frac{T_C}{T_W}}$$

- At the **maximum work condition**
the thermal efficiency:
(Finite-time thermodynamics)

Condition at maximum efficiency and maximum work is different.
That is the contradiction of the performance.

Propose the **normalized** thermal efficiency for low-grade thermal energy conversion

– An application of ORC –

[2] I. I. Novikov, The efficiency of atomic power stations, Nucl. Energy II-7 1958;125-128; Translated from At. Energy. 3; 1957. p. 409

[3] F. L. Curzon and B. Ahlborn, Efficiency of a Carnot engine at maximum power output, Am. J. Phys., Vol. 43; 1975. p.22-24

Applicable heat sources

Low-grade Thermal Energy Conversion (LTEC)



Series of small scale ORC package units commercialized or semi-commercialized in Japan



ULVAC

3 kW



ANEST
IWATA

11 kW



IHI

20 kW



KOBELCO

72 kW



ELECTRA
THERMO

110 kW



ACCESS
ENERGY

135 kW

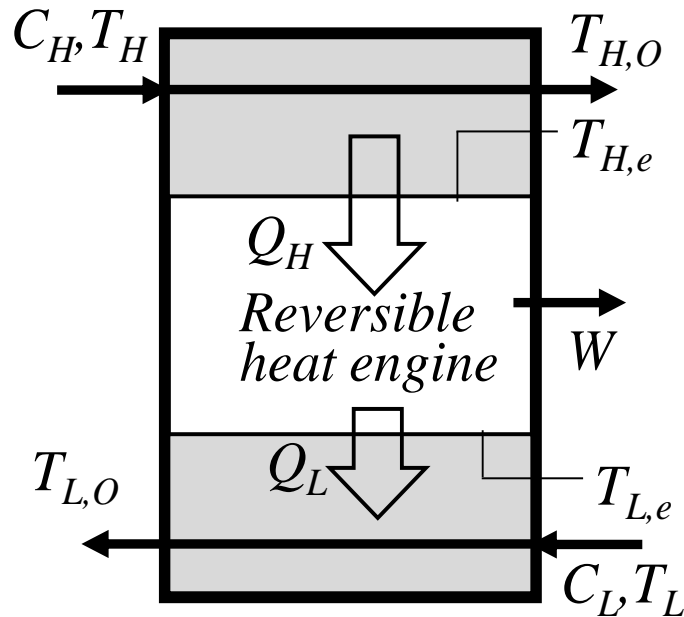
Performance Spec. is only Capacity of Products. Why ?

On the other hand, many researches uses the achievement of increase of the thermal efficiency in their system.

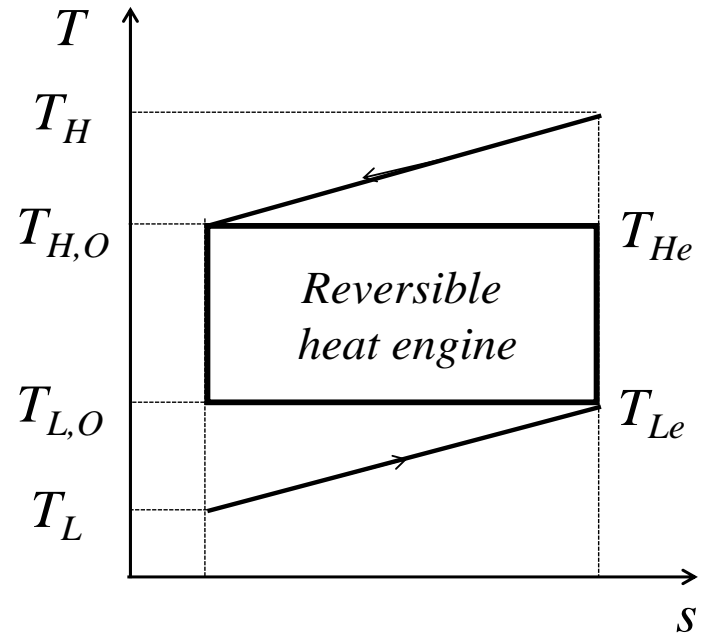
Definition of the effective thermal efficiency is required.

2. Concept

Thermodynamic model of ideal condition



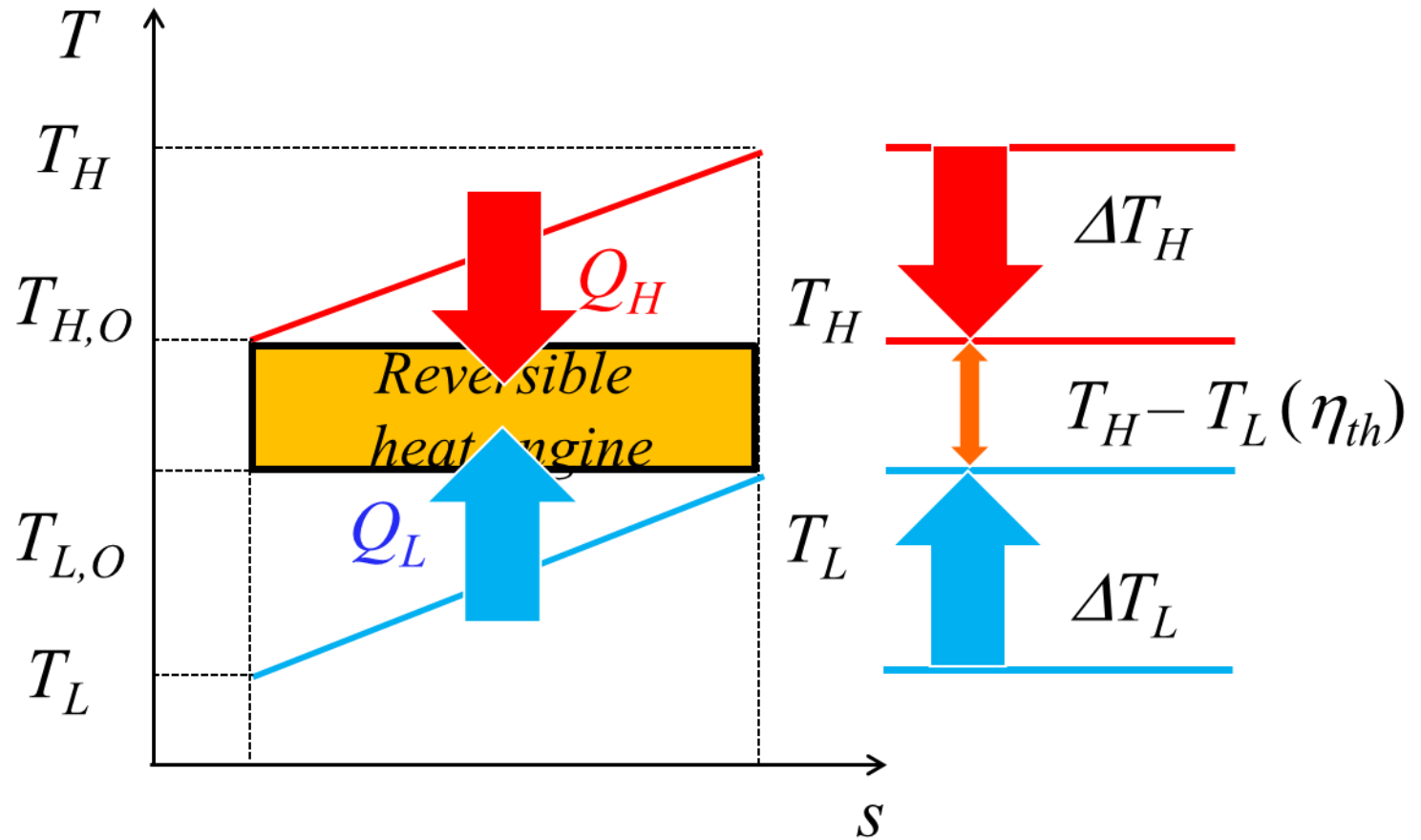
Conceptual model



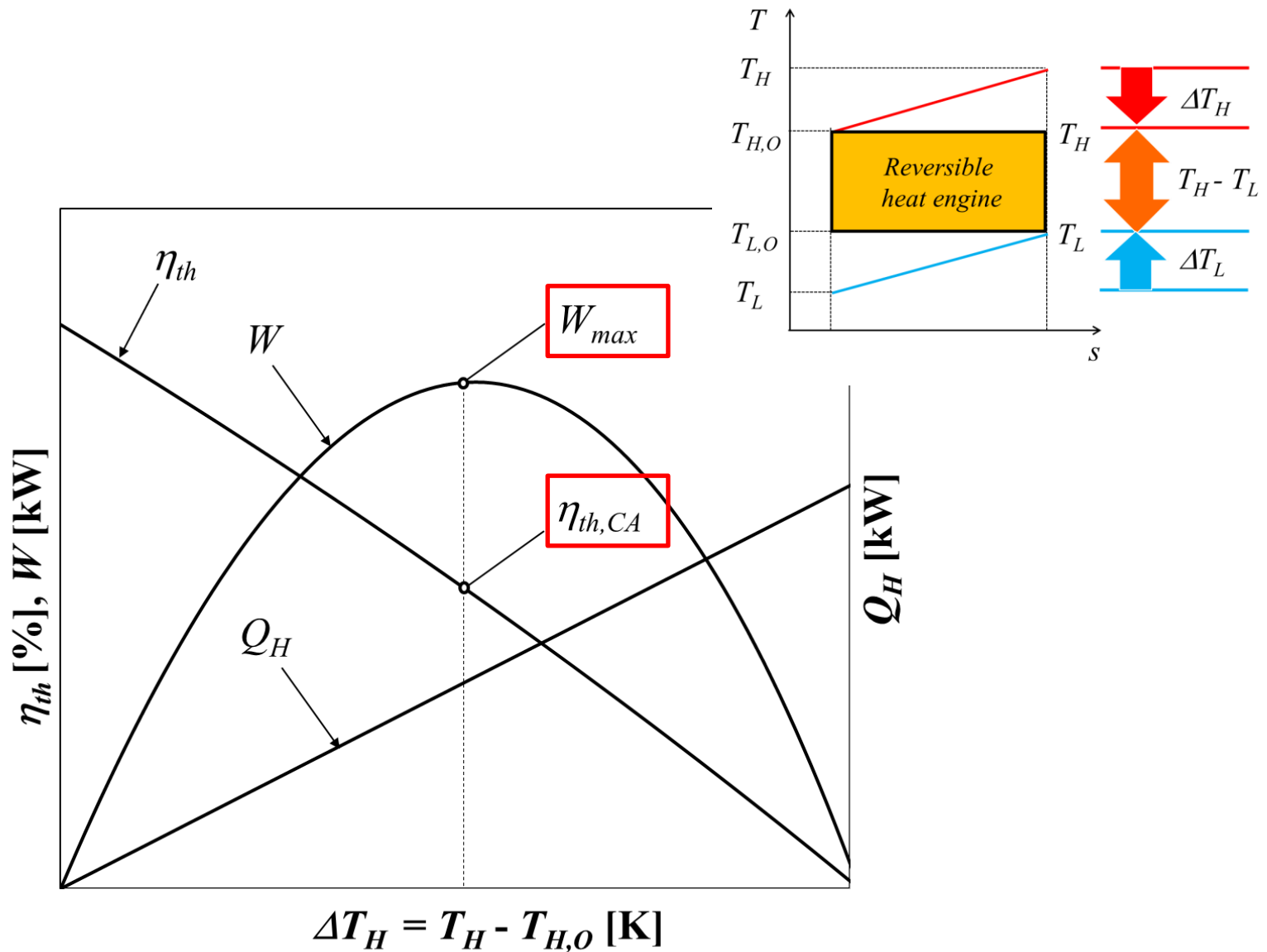
Conceptual T-s diagram

- *Thermal energy is stored in liquid as sensible heat*
- *Specific heat is constant*
- *Ideal heat exchanger (zero pinch temperature)*
- *Reversible heat engine (Carnot cycle)*

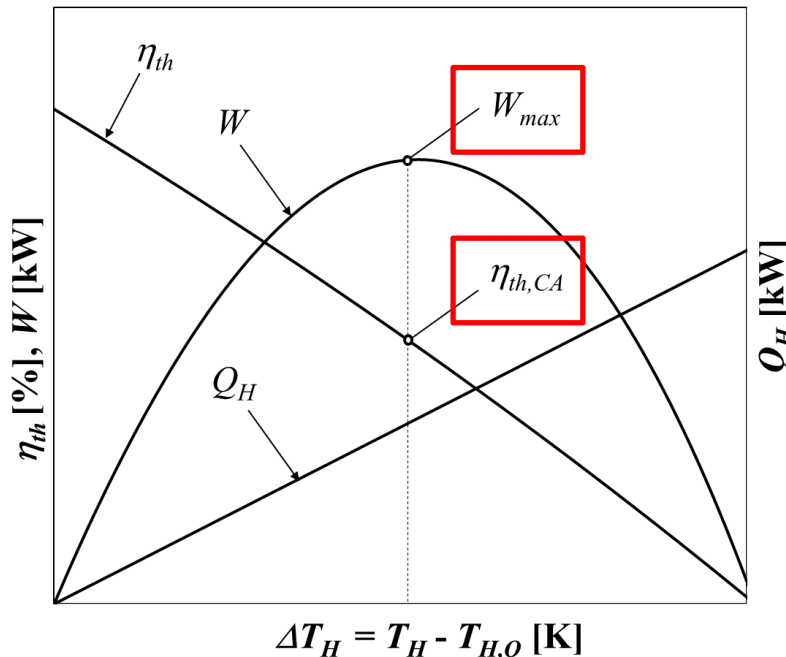
Contradiction of the perk of work and thermal efficiency



Contradiction of the perk of work and thermal efficiency



Maximum work condition



$$Q_H = rC_{HS}(T_H - T_{H,O})$$

$$\eta_{th} = 1 - \frac{T_{L,O}}{T_{H,O}}$$

$$\Delta S = \frac{Q_H}{T_{H,O}} - \frac{Q_L}{T_{L,O}} = 0$$

$$W = \eta_{th}Q_H = f(T_{H,O})$$

W will be the one degree of freedom

$$\frac{\partial W}{\partial T_{H,O}} = 0 \quad \Rightarrow \quad W_{max}$$

$$C_{HS} = C_H + C_L, \quad r = C_H / C_{HS}$$

C is the heat capacity flow rate [W/K]

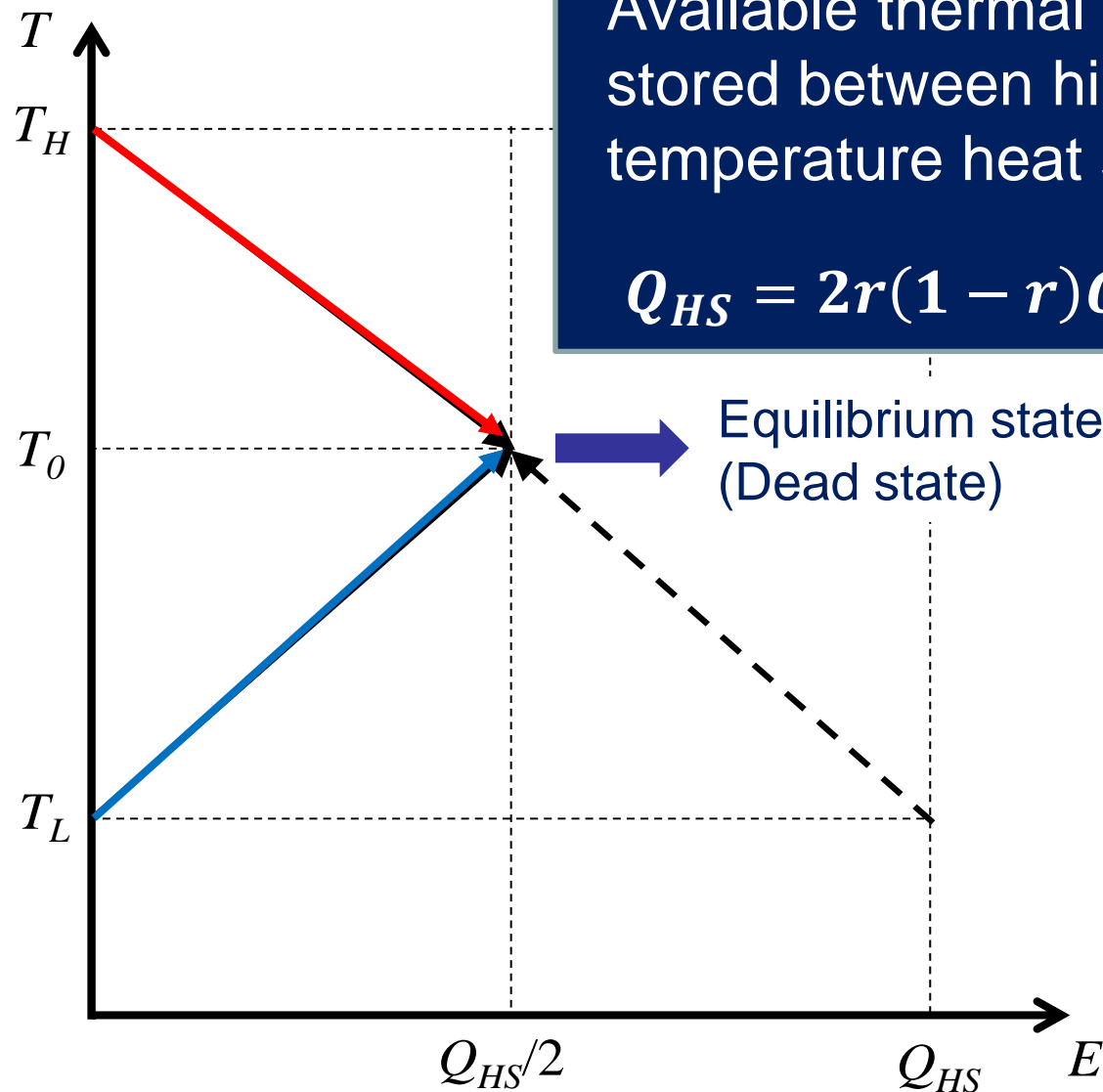
(mass flow rate [kg/s] times specific heat [kJ/kgK])

$$W_{max} = r(1 - r)C_{HS}(\sqrt{T_H} - \sqrt{T_L})^2$$

$$\eta_{th,CA} = 1 - \sqrt{\frac{T_L}{T_H}}$$

3. Normalization of Thermal Efficiency

Thermal energy in heat source



Available thermal energy stored between high and low temperature heat source

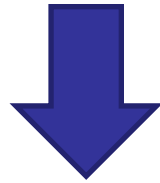
$$Q_{HS} = 2r(1 - r)C_{HS}(T_H - T_L)$$

Equilibrium state
(Dead state)

Normalized thermal efficiency

Conventional thermal efficiency

$$\eta_{th} = \frac{W}{Q_H} = \frac{W}{rC_{HS}(T_H - T_{H,O})}$$



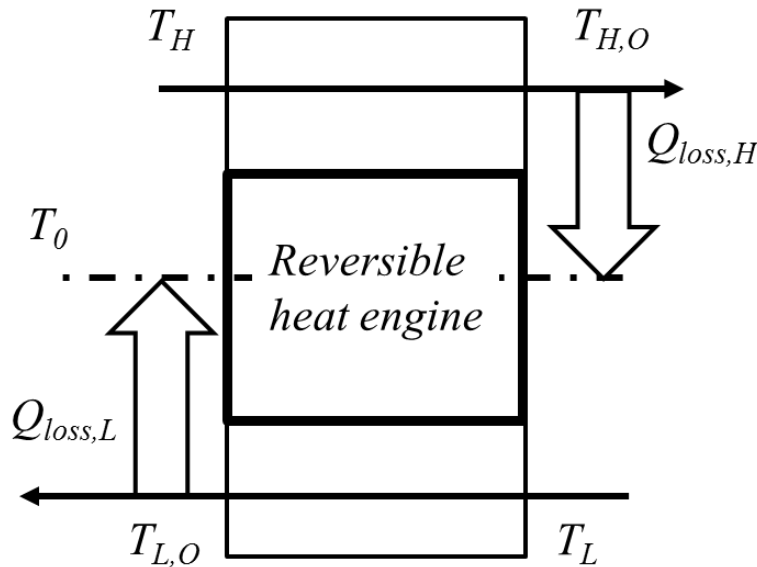
Change the denominator to available thermal energy

$$\eta_{th,Nor} = \frac{W}{Q_{HS}} = \frac{W}{2r(1-r)C_{HS}(T_H - T_L)}$$

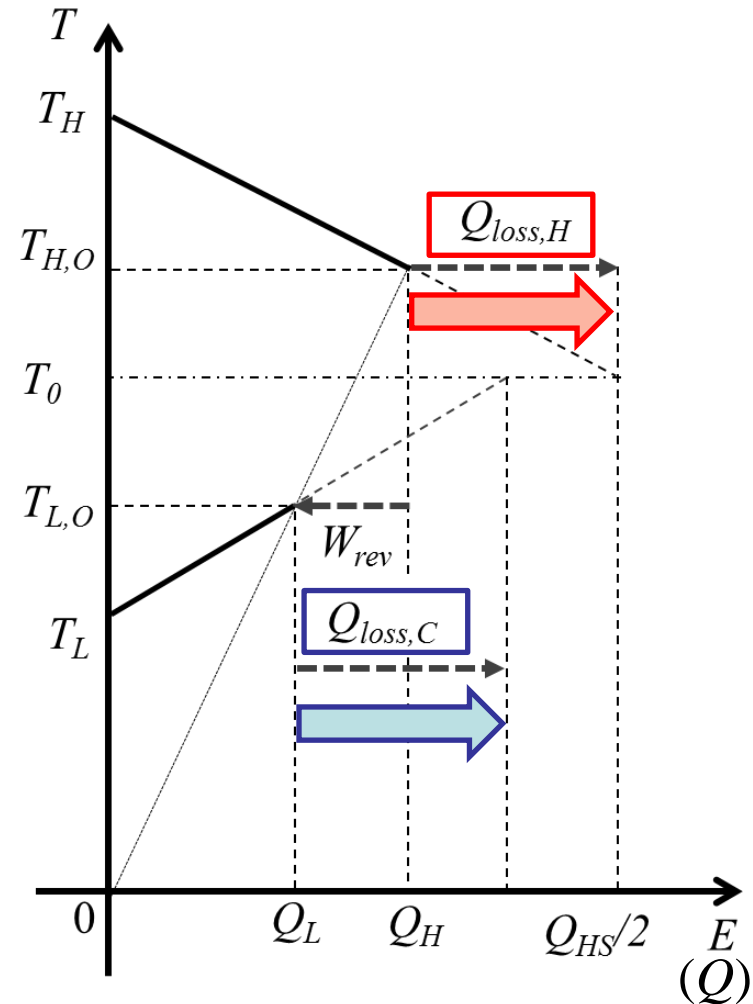
Normalized thermal efficiency

Normalized thermal efficiency only depends on the heat source condition and independent from the heat transfer rate to heat engine

Normalized thermal efficiency takes into account the external irreversibility

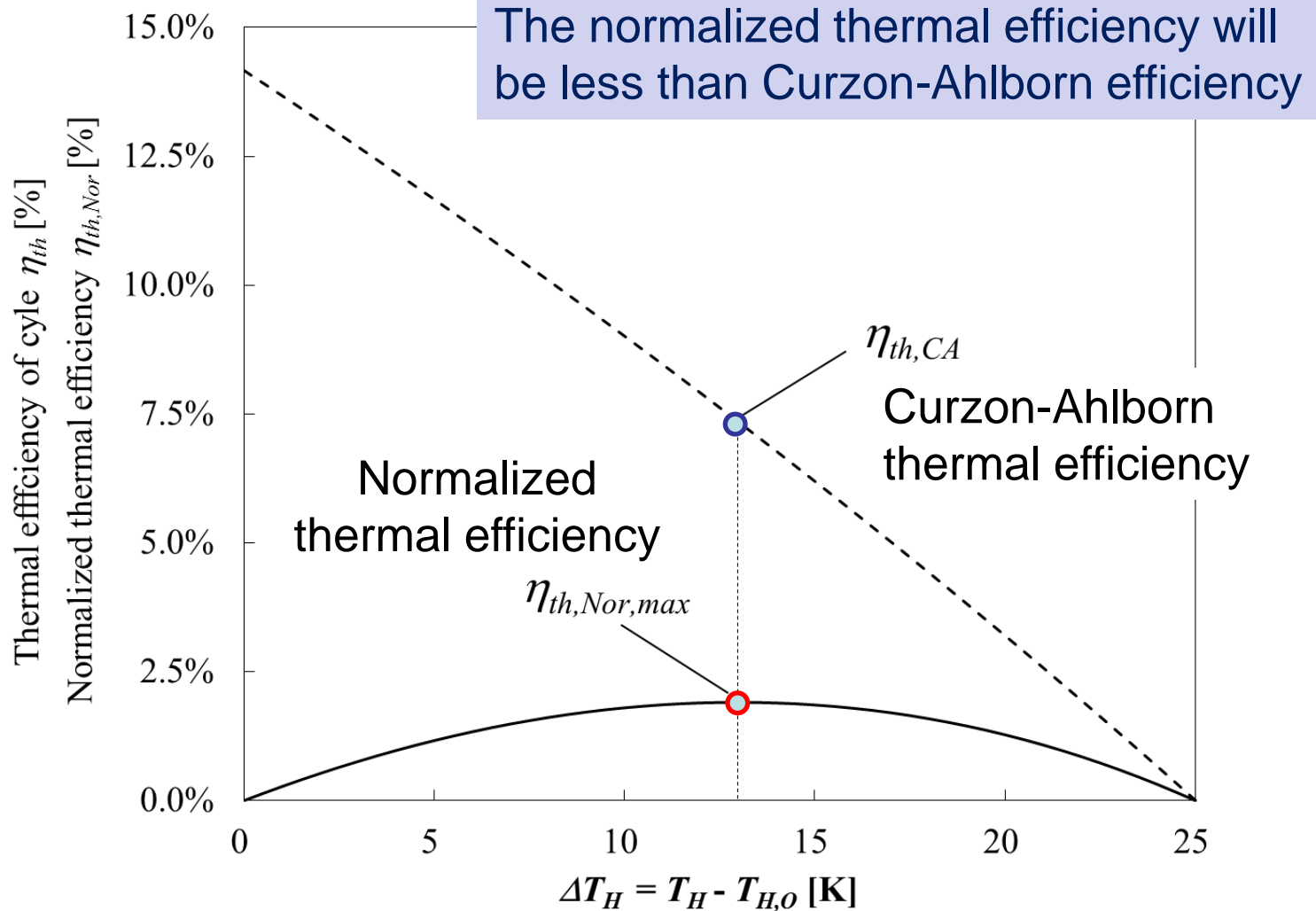


To apply the heat source thermal energy based on the equilibrium state to thermal efficiency is equivalent to take into account the **external irreversibility**



- [11] A. Bejan, Graphic Techniques for Teaching Engineering Thermodynamics, *Mechanical Engineering News*, (1997), pp.26-28
 [12] P. Salamon, K. H. Hoffmann, S. Schubert, R. S. Berry, B. Anderson, What conditions make minimum entropy production equivalent to maximum power production, *J. Non-Equilibrium Thermodynamics*, Vol. 26, (2001), pp.73-83

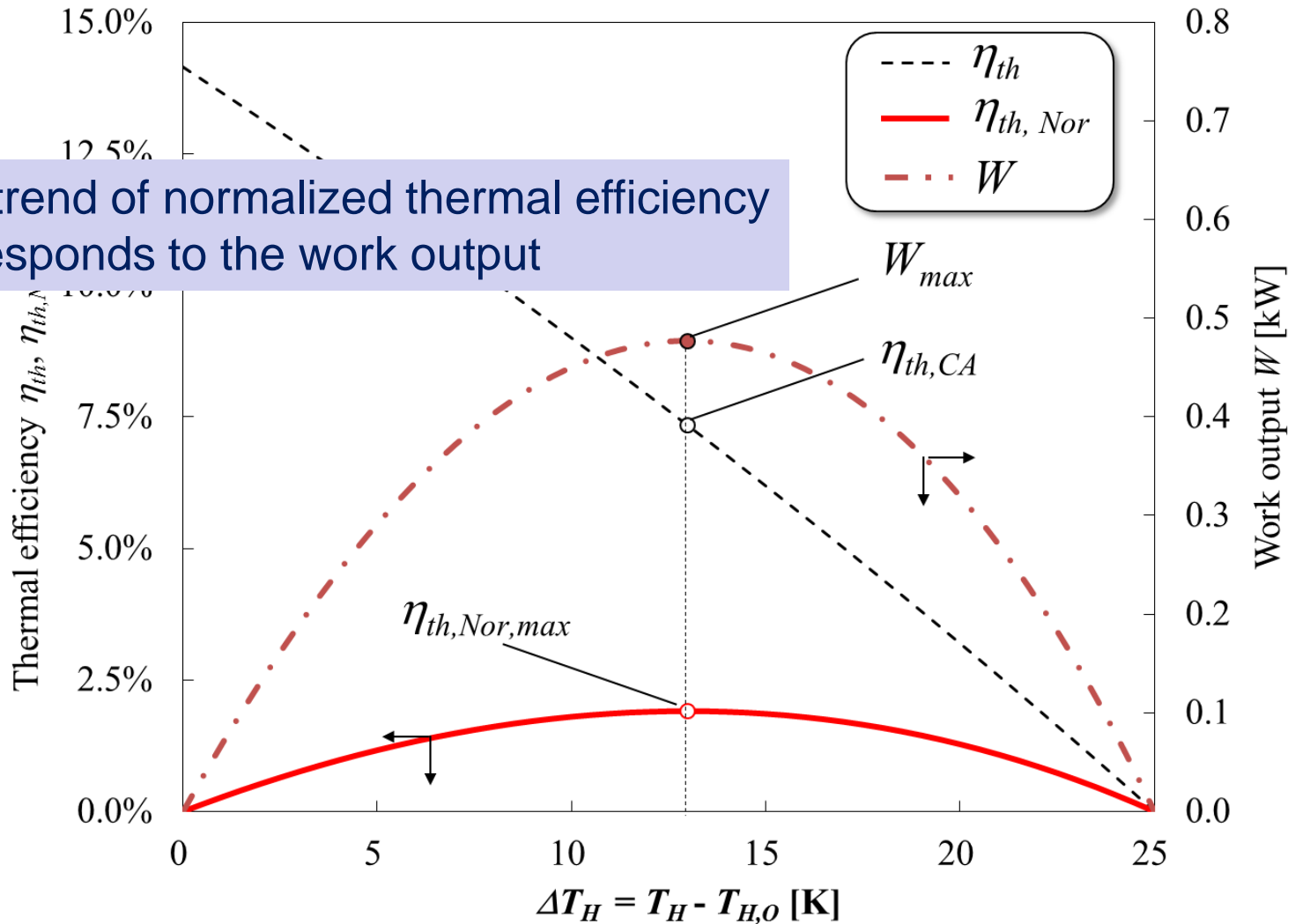
Comparison between normalized thermal efficiency and conventional thermal efficiency



In case $T_H=80^\circ\text{C}$, $T_L=30^\circ\text{C}$, $r=0.5$, $C_{HS}=1$ kW/K.

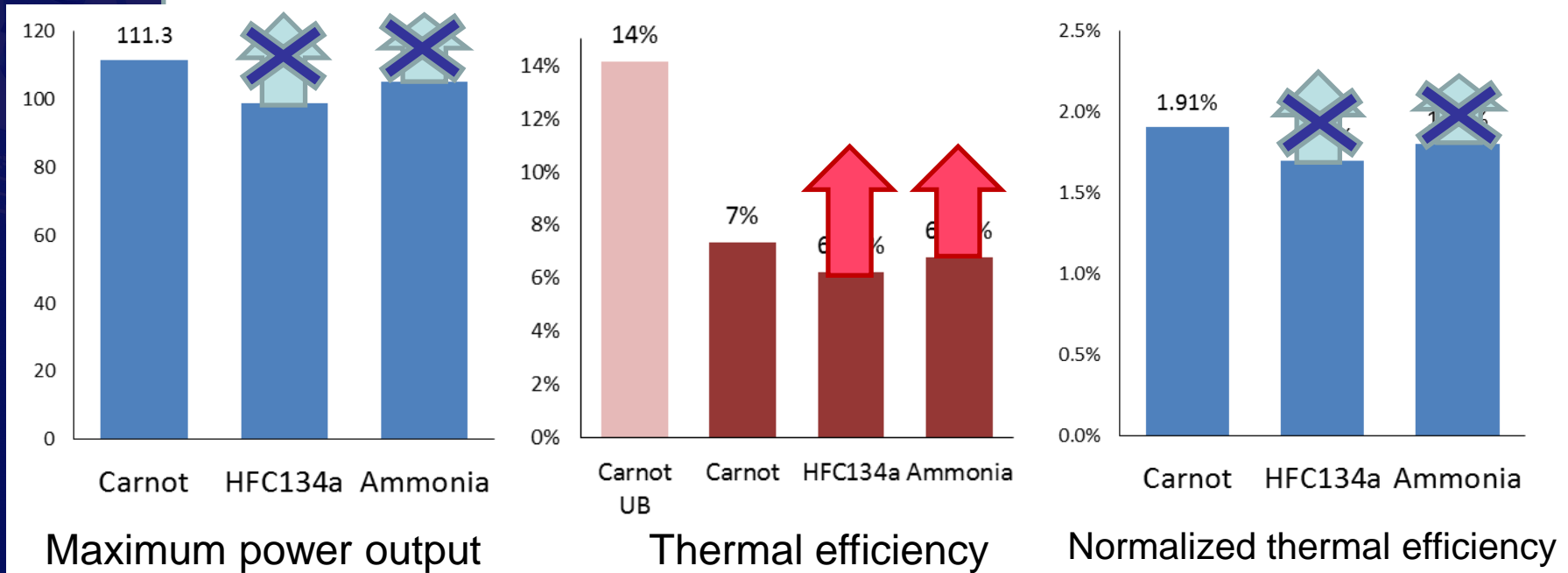
Comparison between normalized thermal efficiency and conventional thermal efficiency

The trend of normalized thermal efficiency corresponds to the work output



In case $T_H=80^\circ\text{C}$, $T_L=30^\circ\text{C}$, $r=0.5$, $C_{HS}=1$ kW/K.

Application of normalized thermal efficiency to Rankine cycles



In the design stage of ORC on LTEC, the **maximization of normalized thermal efficiency will lead to the maximization of work output** from a heat engine, instead of the conventional thermal efficiency.

The heat source condition corresponds to Ref. [15] that $T_H=80\text{ }^\circ\text{C}$, $T_L=30\text{ }^\circ\text{C}$, $C_{HS}=233\text{ kW/K}$.
 [15] T. Morisaki and Y. Ikegami, Maximum power of a multistage Rankine cycle in low-grade thermal energy conversion, *Applied Thermal Engineering*, Vol.69, (2014), pp.78-85

4. Summary and future work

Summary

Still the field of Low-grade thermal energy conversion (LTEC) system uses the thermal efficiency as the performance evaluation and try to achieve higher thermal efficiency.

The effective thermal efficiency is required for the effective evaluation of the system.

In the field of the LTEC, the **normalized thermal efficiency** is proposed and the maximization of normalized thermal efficiency will maximize the power output of the system.

$$\eta_{th,Nor} = \frac{W}{Q_{HS}} = \frac{W}{2r(1-r)C_{HS}(T_H - T_L)}$$

Future work

- To extend the concept to exergy efficiency for Low-grade thermal (Not to misread the normalized thermal efficiency)
- To apply the normalized thermal and exergy efficiencies to the design optimization for Low-grade thermal energy conversion
- To extend the idea to the other heat source systems

Thank you so much for your attention.
Grazie mille

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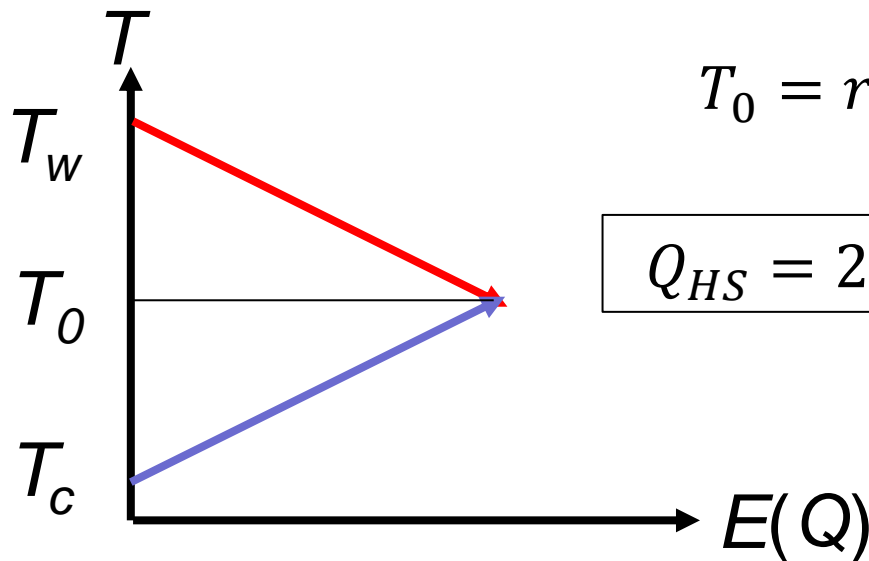


$$Q_{HS} = \underline{(mc_p)_H(T_H - T_{H,o})} + \underline{(mc_p)_L(T_{L,o} - T_L)}$$

$$= \underline{C_H(T_H - T_{H,o})} + \underline{C_L(T_{L,o} - T_L)}$$

$$Q_{HS} = C_H(T_H - \underline{T_0}) + C_L(\underline{T_0} - T_L)$$

T_0 : dead state (Equilibrium state)



$$T_0 = rT_H + (1 - r)T_L$$

$$Q_{HS} = 2r(1 - r)C_{HS}(T_H - T_L)$$